## CCIS 4100: in-class exercise on TDL

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Complete the following either on your own or in small groups.

## Temporal-difference learning



Figure 1: Exciting gridworld (again!) from the text (Figure 17.1). Here we assume that we have populated the grid with  $V^{\pi}$  estimates after some number of observations/trials.

Assume R = -0.1 (i.e., the 'living penalty' – instantaneous reward – is -0.1). This time we don't know the transition probabilities and we don't know the rewards at the outset! – they have to be observed. Further assume that we do not impose a discount ( $\gamma = 1$ ). Remember, the general form of the update is:

$$V^{\pi}(s) \leftarrow (1 - \alpha) V^{\pi}(s) + \alpha \{ R(s, \pi(s), s') + \gamma V^{\pi}(s') \}$$
(1)

1. Assume the agent has run some number of trials already and, using TDL, come up with the V estimates depicted in Figure 2. Suppose you begin now at state (3,3) and observe:

 $(3,3) \to (3,4)$ 

Suppose  $\alpha = 0.1$ . Update the  $V^{\pi}$  estimate for state (3,3).

2. Now assume we observe a transition under  $\pi$  from (2,3) to (2,4); update  $V^{\pi}$  for (2,3).

- 3. Finally, using the updated  $V^{\pi}$  estimates calculated above, assume we observe a transition from  $(2,3) \rightarrow (3,3)$ . Update the  $V^{\pi}$  estimate for (2,3) once more.
- 4. To think about: what would have happened to the  $V^{\pi}$  estimate for (2,3) in steps 2 and 3 if  $\gamma$  were 1? More generally, what sort of properties does a 'good'  $\gamma$  value have for TDL learning?